# A Single-Stage High-Frequency Isolated Secondary-Side Controlled AC-DC Converter

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Abstract—This paper presents a new single-stage highfrequency isolated ac-dc converter that uses a simple control circuit. It is well suitable for wide input variation power sources. The circuit configuration combines a diode rectifier, boost converter and half-bridge dc-dc resonant converter. A high power factor is achieved by discontinuous current mode (DCM) operation of the front-end integrated power factor correction circuit. The output voltage is regulated by fixedfrequency, secondary-side phase-shift active rectifier. Softswitching operation is achieved for all the switches. This converter operates in three modes, which is classified according to conduction of different switches and diodes. The intervals of operation and steady-state analysis are presented in detail. Design example of a 100 W proposed converter is given together with its simulation and experiment results for wide variation in input voltage.

Index Terms—single-stage, ac-dc converter, DCM, active rectifier, high-frequency isolation, soft-switching

#### I. Introduction

Single-phase high-frequency (HF) transformer isolated ac-to-dc converters used in many applications [1-7] ask for following performances: wide variable input range, high power factor and low distortion in ac line current; compact size, simple control strategy and high efficiency. One such application is Permanent Magnet Synchronous Generator (PMSG) based small Wind Energy Conversion System (WECS). The well known conventional approach uses three stages of power conversion: front-end two-stage circuit consisting of a rectifier and a boost converter for power factor correction (PFC) followed by a HF transformer isolated half/ full-bridge dc-to-dc converter as the third stage. This type of approach uses many components resulting in larger size with higher cost and low efficiency. Two approaches are available to reduce the number of stages from three to two and to get improved efficiency: (a) Front-end diode rectifier followed by an integrated dc-dc converter that handles both PFC and HF isolation [1-2]. (b) Introduce active rectifier that achieves PFC instead of uncontrolled diode rectifier followed by HF isolated dc-dc converter [2-5].

Efforts to achieve all the expected functions in a single-stage are reported in [6-7]. In [6], the diode rectifier is integrated with a HF isolated half-bridge resonant converter to form a dual-switch circuit. In [7] two buck-boost dc-dc converters are integrated with two diode rectifiers at the front-end for PFC function and they share switches with a full-bridge series resonant HF isolated dc-dc converter. A high power

factor is achieved in [6-7] by operating the input line side in discontinuous current mode (DCM) [8] and the output voltage regulation is achieved by a wide variation in switching frequency. These configurations require a wide variation (almost 2:1) in switching frequency for power control. The dc bus voltage also increases significantly with the increased switching frequency.

Wide variation in switching frequency for power control makes filter design difficult while introducing higher losses at increased frequencies. A higher dc bus voltage results in the requirement of higher voltage devices increasing the conduction losses. To avoid these problems, a single-stage ac-dc converter is proposed in this paper that uses a fixed frequency phase-shift control technique for output voltage regulation.

The concept of secondary-side phase-shift active rectifier used in dc-dc converters [9] is utilized in realizing a fixed-frequency single-stage ac-dc converter. Also, a resonant converter is used in the proposed circuit for guaranteed soft-switching operation.

#### II. Proposed converter and its operation

The proposed single-phase active rectifier is shown in Fig. 1. At the input side, the diode rectifier is integrated with boost and half-bridge converters to form an integrated rectifier-boost-half-bridge converter  $(D_{r1}, D_{r2}, S_1, S_2, L_1)$ . The PFC can be achieved by DCM operation of the dual-switch boost converter. A low-pass filter  $(L_f$  and  $C_f$ ) is used for removing HF current harmonics at the ac input line.

A large filter capacitor  $(C_{bus})$  is used to obtain a constant dc bus voltage  $(V_{bus})$ . Switches  $(S_1, S_2)$  in PFC circuit are shared with a half-bridge resonant converter, which includes two capacitors  $(C_1, C_2)$  and a resonant tank circuit  $(L_r, C_r)$  placed on the primary-side of HF transformer  $T_1$ . A HF active rectifier on the secondary side of  $T_1$  is realized by switches  $S_3$ ,  $S_4$  and diodes  $D_{r3}$ ,  $D_{r4}$ . The operation of the converter is presented next

Fixed-frequency complementary gating signals  $(v_{gs1}, v_{gs2})$  and  $(v_{gs3}, v_{gs4})$  of 50% duty cycle and with a small dead-time between them are applied to  $S_1$  and  $S_2$  on the primary-side and to  $S_3$  and  $S_4$  on the secondary-side (Fig. 2).  $D_{r1}, D_1, S_1$  and  $D_2$  handle the positive half-cycle of input voltage.  $D_{r2}, D_2, S_2$  and  $D_1$  serve for the negative half-cycle of input voltage. A high power factor can be achieved by DCM operation in  $L_1$  over the entire line frequency cycle. Both switches operate in zero-voltage switching (ZVS) mode eliminating the turn

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-on switching losses because of the resonant tank circuit. The output voltage can be regulated by the phase-shift between two legs of switches  $(S_1/S_2)$  and  $S_3/S_4$ .

Based on the relationship between phase-shift angle  $\theta$  and lagging angle  $\beta$  between  $v_{ab}$  and  $i_r$ , the proposed converter operates in three modes. Only positive half-cycle of input waveform is considered due to the symmetrical structure. To simplify the operation and analysis, following assumptions are made: (a) All semiconductors and passive components are ideal. (b) Leakage inductance of HF transformer is part of resonant inductor  $L_r$  and the effect of magnetizing inductance is neglected. (c) Effects of small dead-gaps between two groups of complementary signals are neglected. Capacitors  $C_{bus}$ ,  $C_1$ ,  $C_2$  and  $C_o$  are assumed to be large enough so that the dc bus voltage  $V_{bus}$  and output voltage  $V_o$  can be regarded as constant values.

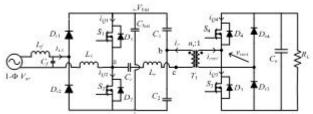


Figure 1. Proposed high-frequency transformer isolated singlephase ac-dc converter

# A. Mode 1, $\theta < \beta$

When  $\theta < \beta$ ,  $S_1$  and  $S_2$  turn-on with ZVS, whereas,  $S_3$  and  $S_4$  turn-off with zero-current-switching (ZCS). The secondary-side HF active rectifier input voltage  $v_{rect}$  is a quasi-square waveform because a free-wheeling current flows through the secondary-side of  $T_1$ . To understand the operation details of mode 1, the steady-state operation waveforms with a certain value of  $\theta$  are given in Fig. 2. There are 8 operating intervals in one HF switching period. Devices conducting during different intervals are also marked in Fig. 2. Equivalent circuit for each interval of operation is shown in Fig. 3.

**Interval 1** ( $t_0$ - $t_1$ ): This interval (Fig. 3a) starts when gating signal  $v_{gs1}$  is applied at  $t=t_0$ , gating signal  $v_{gs4}$  remains on ( $v_{gs2}$  and  $v_{gs3}$  are off). During this interval, the current flows through  $D_{r1}$  from the ac source. The voltage between a and b ( $v_{ab}$ ) is positive and is equal to  $V_{bus}/2$ . The current  $i_{L1}$  through boost inductor  $L_1$  starts to increase linearly from zero.  $D_1$  conducts because the resonant current  $i_r$  is negative during the interval. Since  $i_{rect}$  and  $i_r$  are 180° out of phase,  $D_4$  and  $D_{r3}$  are conducting on the secondary-side of  $T_1$ , hence the HF controlled rectifier input voltage ( $v_{rect} = V_o$ ) is positive and the power is delivered to the load. This interval ends when  $v_{gs4}$  is removed ( $S_4$  turns off) and  $v_{gs3}$  is given at  $t_1$ .

**Interval 2**  $(t_1-t_2)$ : The devices conducting on the primary-side of  $T_1$  is the same as previous interval. Since  $v_{gs3}$  is applied,  $S_3$  turns-on and the current flows through  $S_3$  and  $D_{r3}$  that result in a free-wheeling loop on the secondary-side of  $T_1$  (Fig. 3b).  $v_{rect}$  becomes zero and no power is delivered to the load. This interval ends when  $i_r$  reduces to zero at  $t_2$  and  $S_3$  as well as  $D_{r3}$  turns-off with ZCS. Boost inductor current  $i_{L1}$  continues to increase linearly.

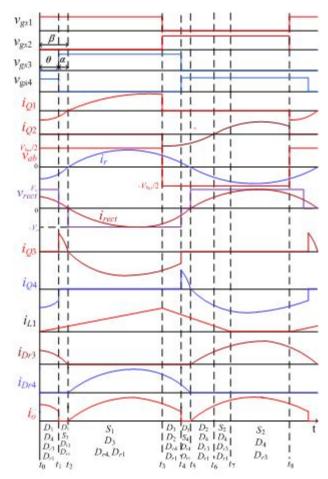


Figure 2. Steady-state waveforms of the proposed converter in one HF cycle for Mode 1 ( $\theta < \beta$ ).

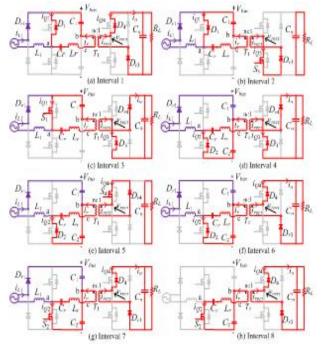


Figure 3. Steady-state equivalent circuits of the proposed converter in one HF cycle for Mode 1.



**Interval 3** ( $t_2$ - $t_3$ ): When  $i_r$  becomes positive,  $S_1$  turns on with ZVS mode. On the secondary-side,  $D_3$  turns-on allowing the current to flow through  $D_3$  and  $D_{r_4}$  and power is delivered to the load (Fig. 3c). Current  $i_{L_1}$  continues to increase linearly in this interval and reaches its peak value when  $v_{gs1}$  to  $S_1$  is removed at  $t_3$ . Half of one HF switching cycle has ended at the end of this interval.

**Interval 4**  $(t_3$ - $t_4$ ): This interval starts when  $v_{gs1}$  is removed and  $v_{gs2}$  is applied.  $v_{ab}$  changes its polarity from positive to negative,  $v_{ab} = -V_{bus}/2$ . On primary-side of  $T_1$ , since  $S_1$  is turned-off  $D_2$  begins to conduct (Fig. 3d), and  $i_{L1}$  decreases linearly from its peak value. Power continues to be delivered to the load through  $D_3$  and  $D_{r4}$ . The interval ends when gating signal  $v_{as3}$  is removed.

**Interval 5** ( $t_4$ - $t_5$ ): Since  $v_{gs3}$  is removed and  $v_{gs4}$  is applied at the beginning of this interval,  $S_4$  turns-on and the current flows through  $S_4$  and  $D_{r4}$  that result in a free-wheeling loop on the secondary-side of  $T_1$  (Fig. 3e).  $v_{rect}$  becomes zero and no power is delivered to the load. The devices conducting on the primary-side of  $T_1$  are the same as previous interval. This interval ends when  $i_r$  goes to zero at  $t_5$ ,  $S_4$  and  $D_{r4}$  turns-off with ZCS and  $i_{L1}$  continues to decrease linearly.

**Interval 6**  $(t_5 - t_6)$ : In this interval, the polarity of  $i_r$  has changed from positive to negative. On the secondary-side of  $T_1$ ,  $D_4$  and  $D_{r3}$  turn-on with ZCS and power is supplied to the load (Fig. 3f). At  $t = t_6$ ,  $i_{Q2}$  (i.e. current through  $D_2$ ) reaches zero and current  $i_{L1}$  continues to decrease linearly.

**Interval 7** ( $t_6$ - $t_7$ ): At  $t = t_6$ ,  $S_2$  turns on with ZVS mode. The other devices conducting remain the same as Interval 6 (Fig. 3g). At the end of this interval,  $t = t_7$ ,  $i_{L1}$  decreases to zero and  $D_{r1}$  turns-off with ZCS.

**Interval 8**  $(t_7 - t_8)$ : Since  $D_{r1}$  and  $D_{r2}$  are not conducting,  $i_{L1} = 0$ .  $S_2$  is conducting and energy stored in the circuit is still delivered to the load through  $D_4$  and  $D_{r3}$  (Fig. 3h). At  $t = t_8$ , one HF switching cycle has completed and next cycle begins.

#### B. Mode 2, $\theta = \beta$

In this mode,  $S_1$  and  $S_2$  operate with ZVS turn-on. The HF active rectifier works as a typical diode rectifier. Current flows only through  $D_3$  and  $D_4$ , switches  $S_3$  and  $S_4$  do not conduct even though  $v_{gs3}$  and  $v_{gs4}$  are applied. The secondary-side HF active rectifier input voltage ( $v_{rect}$ ) is a square waveform since there is no free-wheeling interval. Therefore, energy is delivered to the load continuously. All currents and voltages on the secondary side of  $T_1$  are the same as those when a diode rectifier is used on the secondary-side of  $T_1$ . The details of the Mode 2 will not be presented here.

# *C.* Mode 3, $\theta > \beta$

If  $\theta$  is larger than  $\beta$ , all the switches,  $S_1$  -  $S_4$ , operate with ZVS turn-on. On the secondary-side, HF active rectifier input voltage  $v_{rect}$  is a quasi-square waveform because a freewheeling current flows through the secondary-side of  $T_1$ . In this mode, there are 7 operating intervals in one HF switching period as shown in the steady-state waveforms of Fig. 4. Devices conducting during different intervals are also marked in Fig. 4 and equivalent circuits for operation are

shown in Fig. 5.

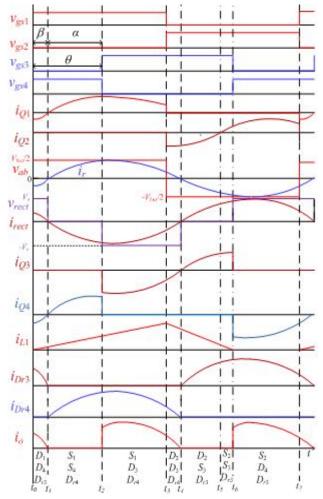


Figure 4. Steady-state waveforms of the proposed converter in one **HF cycle for Mace 3** ( $\theta > \beta$ ). Note:  $D_{r1}$  is conducting for intervals 1 to

**Interval 1** ( $t_0$ - $t_1$ ): Operation of this interval (Fig. 5a) is same as interval-1 of Mode 1. This interval ends when  $i_r$  and  $i_{rect}$  reach zero at  $t_2$ , hence  $i_{Q1}$  and  $i_{Q4}$  also reach zero turning off  $Q_1$  and  $Q_4$  with ZCS. Also,  $D_{r3}$  turns-off with ZCS and  $D_{r4}$  turns-on with ZCS.

**Interval 2**  $(t_1 - t_2)$ : In this interval (Fig. 5b), since gating signals have been already given to  $S_1$  and  $S_4$  both turn on with ZVS mode. On the secondary-side of  $T_1$ , free-wheeling current flows through  $D_{r4}$  and  $S_4$ , resulting in zero voltage across the secondary winding,  $v_{rect} = 0$ . This interval ends when the gating signal  $v_{gs4}$  is removed and  $v_{gs3}$  is given to  $S_3$  at  $t_2$ , current  $i_{L1}$  continues to increase linearly.

**Interval 3**  $(t_2$ - $t_3$ ): Since  $v_{gs4}$  is removed and  $v_{gs3}$  was given to  $S_3$  at the end of last interval,  $S_4$  turns-off and  $D_3$  starts conducting together with  $D_{r4}$  (Fig. 5c) delivering power to the load. Gating signal  $v_{gs1}$  to  $S_1$  is removed at  $t_3$ . Boost inductor current  $i_{L1}$  continues to increase linearly in this interval and reaches its peak value at  $t_3$ .

**Interval 4** ( $t_3$ - $t_4$ ): Since  $v_{gs1}$  was removed and  $v_{gs2}$  was given to  $S_2$  at  $t_3$ , the polarity of  $v_{ab}$  changes from positive to negative,  $v_{ab} = -V_{bus}/2$ .  $D_2$  starts to conduct and  $i_{L1}$  begins to decrease side of  $T_1$  remains the same as interval 3 (Fig. 5d). Power is still delivered to the load.

This interval ends when  $i_r$  and  $i_{rect}$  reach zero at  $t_4$ , hence  $i_{O3}$  and  $i_{DR4}$  also reach zero, i.e.,  $D_3$ ,  $D_{r4}$  turn off with ZCS.

Interval 5 ( $t_4$ - $t_5$ ): The devices conducting on the primary-side of  $T_1$  are the same as previous interval.  $S_3$  turns on with ZVS mode and the current flows through  $S_3$  and  $D_{r3}$  that result in a free-wheeling loop on the secondary-side of  $T_1$  (Fig. 5e).  $v_{rect}$  becomes zero and no power is delivered to the load. Current  $i_{L1}$  continues to decrease linearly and  $i_{Q2}$  becomes zero ( $D_2$  turns off with ZCS) at the end of this interval.

**Interval 6** ( $t_5$ - $t_6$ ): Since gating signal is already given to  $S_2$ ,  $S_2$  is turned on with ZVS mode since current through its antiparallel diode reached zero at the end of last interval. On the secondary-side, devices conducting are the same as last interval with  $v_{rect} = 0$  and no output power is delivered (Fig. 5f). At  $t = t_6$ ,  $i_{L1}$  decreases to zero and  $D_{r1}$  turns-off with ZCS.

**Interval 7**  $(t_6-t_7)$ : This interval (Fig. 5g) is the same as the interval-8 of Mode 1. At  $t = t_7$ , one HF switching cycle has completed and it is ready for next cycle.

The intervals shown above are for certain values of phase-shift for three typical modes. If different values of phase-shift are given, sequence of intervals might be different, but the soft-switching operation in these modes is guaranteed.

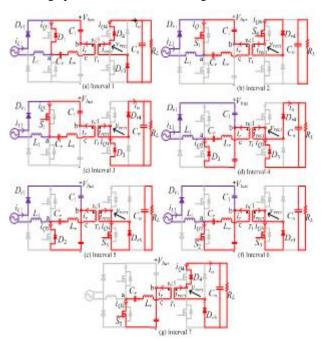


Figure 5. Steady-state equivalent circuits of the proposed converter in one HF cycle for Mode 3.

#### III. STEADY-STATE ANALYSIS

For analysis purpose, the single-stage converter can be viewed as two separate parts: (i) front-end PFC circuit and (ii) half-bridge resonant converter with secondary-side HF active rectifier. The PFC circuit operates in DCM mode and its analysis is well known [2,8].

The steady-state analysis of the half-bridge resonant converter with secondary-side HF active rectifier is done using approximate analysis (i.e., using fundamental components in the Fourier series of waveforms, neglecting higher

harmonics) approach [10,11] and is presented next.

All parameters on the secondary-side of the HF transformer are reflected to primary side of  $T_1$ , which are denoted by the superscript "' ". To get generalized design curves, all the parameters are normalized using the base values:  $V_B = V_{bus,max}/2$ ,  $Z_B = R'_L$ ,  $I_B = V_B/Z_B$ . The Half-bridge converter gain is defined as  $M = V_O'/(0.5V_{bus})$ . The normalized switching frequency is given by  $F = \omega_s/\omega_r = f_s/f_r$  where resonant frequency  $\omega_r = 2\pi f_r = 1/(\sqrt{L_r C_r})$  and switching frequency,  $f_s = \omega_s/(2\pi)$ . The normalized values of all reactances are given by  $X_{Lr,pu} = QF$ ,  $X_{Cr,pu} = -Q/F$ ,  $X_{s,pu} = X_{Lr,pu} + X_{Cr,pu} = Q(F - 1/F)$ , where  $Q = \omega_r L_r/R'_L$ .

Since it is preferred that all switches operate in ZVS mode, the proposed converter should preferably operate in Mode 2 and Mode 3. Therefore, the following analysis presented is based on the preferred modes 2 and 3.

In the approximate analysis first step is to replace the HF active rectifier by ac equivalent impedance ( $Z_{ac}$ ). Fig. 6 shows the HF active rectifier diagram with all voltages and currents referred to primary-side of  $T_1$ . Assume  $V'_o$  is constant due to the large filter capacitor across the load.  $\beta$  is the lagging angle between  $V_{ab}$  and  $i_r$ , and  $\theta$  is the controlled phase-shift angle. The HF active rectifier input voltage  $V'_{rect}$  is a quasisquare wave with an amplitude of  $\pm V'_o$  and pulse width of  $(\pi+\beta-\theta)$ . Resonant current  $i_r$  lags the voltage  $v_{ab}$  by  $\beta$  and fundamental component of  $V'_{rect}$  lags  $v_{ab}$  by

 $[\beta + \frac{\theta - \beta}{2}] = (\theta + \beta)/2. \text{ Define } \alpha = (\theta - \beta), (\pi + \beta - \theta) = (\pi - \alpha).$ 

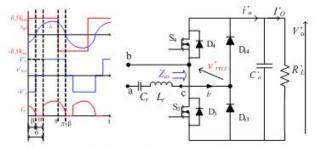


Figure 6. Voltages and currents in HF active rectifier, all parameters referred to primary-side.

The equations for the instantaneous values of fundamental components of the voltage  $(v_{ab})$  across the output terminals a and b; resonant current i; and rectifier input voltage  $(v'_{rect})$  referred to primary-side are given by

$$v_{ab1} = \sqrt{2}V_{ab1}\sin(\omega_s t) = \sqrt{2}\frac{4(V_{bus}/2)}{\sqrt{2}\pi}\sin(\omega_s t) \text{ V},$$
 (1)

$$i_r = \sqrt{2}I_r \sin(\omega_s t - \beta)$$
 A, (2)

$$v'_{rect1} = \sqrt{2}V'_{rect1}\sin\left(\omega_s t - (\beta + \frac{\alpha}{2})\right)$$
 V, (3)

where  $V_{ab1}$  = rms value of fundamental component of  $v_{ab}$ ,  $I_r$  = rms value of the resonant current, and  $V'_{rect1}$  = rms value of the fundamental component of  $v'_{rect}$  given by

$$V'_{rect1} = \frac{4V'_0}{\sqrt{2}\pi} sin\left(\frac{\pi + \beta - \theta}{2}\right) = \frac{4V'_0}{\sqrt{2}\pi} cos\left(\frac{\alpha}{2}\right)$$
 V. (4)

If  $\theta = \beta$ , the active rectifier operates in Mode 2, i.e., it acts as a diode rectifier. The load current  $I'_{\alpha}$  is the average value of  $i'_{\alpha}$ , which is obtained as

$$I'_{o} = \frac{1}{\pi} \int_{\theta}^{\pi+\beta} \sqrt{2} I_{r} \sin(\omega_{s} t - \beta) d\omega_{s} t = \frac{2\sqrt{2} I_{r}}{\pi} \cos^{2}\left(\frac{\alpha}{2}\right) A$$
 (5)

So the rms value of HF rectifier input (same as the resonant) current  $i_{j}$  is given by

$$I_r = \frac{\pi \, I_0}{2\sqrt{2}\cos^2\left(\frac{\alpha}{2}\right)} \qquad \qquad A \tag{6}$$

Note that  $V'_{rect}$  and  $i_r$  are not in phase, so the ac impedance (looking into terminals "bc") can be written as

$$Z_{ac} = \frac{V_{rect_1} \angle - (\beta + \alpha/2)}{I_r \angle - \beta} = |Z_{ac}| \angle \frac{-\alpha}{2} \qquad \Omega$$
 (7)

Using (4) and (6)

$$|Z_{ac}| = \frac{V_{rsct1}}{l_r} = \frac{8R'_L}{\pi^2} cos^3 \left(\frac{\alpha}{2}\right)$$
 (8)

where primary side referred load resistance,  $R'_{I} = V'_{I}/I'_{I} \Omega$ . The output power (assumed to be same as the rectifier input power since losses are neglected) is given by

$$P_o = V'_{rect1} I_r cos(\alpha/2)$$
 W (9)

The half-bridge converter voltage gain in the phasor circuit shown in Fig. 7 can be evaluated as follows:

$$\left| \frac{V_{I_{rect1}}}{V_{ab1}} \right| = \frac{|Z_{ac}|}{|Z_{ac} + jX_{S}|} = \frac{1}{\left| A^{2} + \left( \frac{\pi^{2}Q(F - 1/F)}{8A^{3}} - \sqrt{1 - A^{2}} \right)^{2} \right|}$$
(10)

where  $X_s = Q(F - 1/F)R'_L$ , and  $A = \cos(\alpha/2)$ Also using (1) and (4),

$$\frac{V'_{rect1}}{V_{ab1}} = \frac{V'_{o}}{0.5V_{bus}} \cos\left(\frac{\alpha}{2}\right) \tag{11}$$

Therefore using (10) and (11), the normalized half-bridge voltage gain M (output voltage to bus voltage) is given by the following expression

$$M = \frac{V_0'}{0.5V_{bus}} = \frac{1/A}{\sqrt{A^2 + \left(\frac{\pi^2 Q(F - 1/F)}{8A^3} - \sqrt{1 - A^2}\right)^2}}$$
(12)

Using (1), the normalized tank peak current is

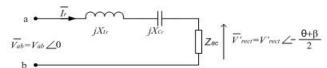


Figure 7. Phasor equivalent circuit of the half-bridge converter used for

$$I_{rp,pu} = \frac{\sqrt{2}V_{ab1,pu}}{|Z_{ac,pu} + jX_{s,pu}|} = \frac{\pi}{2A^3 \left[A^2 + \left(\frac{\pi^2 Q(F-1/F)}{sA^2} - \sqrt{1-A^2}\right)^2\right]}$$
(13)

Then the normalized resonant capacitor peak voltage is

$$V_{crp,pu} = I_{rp,pu} X_{Cr,pu} = I_{rp,pu} (Q/F) \quad \text{p.u.}$$
 (14)

The angle  $\beta$  between  $v_{ab}$  and  $i_r$  is obtained as

$$tan\beta = \frac{\pi^2 Q (F - 1/F)}{8A^4} - \frac{\sqrt{1 - A^2}}{A}$$
 (15)

In this case,  $V_{\text{bus}}$  decreases with increasing value of  $\theta$  due to the fixed duty cycle of gating signals applied to S<sub>1</sub>/S<sub>2</sub>. According to (8), the load of the proposed ac-dc converter  $|Z_{ac}|$  changes with  $\theta$  rising. In order to find the relationship between  $V_{\text{bus}}$  and  $\theta$ , power balance concept (assuming 100%) efficiency) is employed as follows: the ac input real power  $P_{in}$ is given by [2, 8].

$$P_{in} = \frac{V_m^2 D^2 y}{2 \pi L_1 f_2}$$
 W(16,a)

where  $V_m$  is peak value of ac input voltage, D=0.5 is the duty cycle of  $S_1/S_2$ , y is a function of  $V_m/V_{bus}$ . The ac-dc converter output is given by

$$P_o = \frac{V_o^2}{R_L} = \frac{(0.5V_{bus}M/n_t)^2}{R_L}$$
 W(16,b)

Assuming an ideal case (100% of efficiency),  $P_{in} = P_{a}$ , we obtain

$$\frac{V_m^2 D^2 y}{2 \pi L_1 f_s} = \frac{(0.5 V_{bus} M/n_t)^2}{R_L}, \qquad W(17,a)$$

Equation (17a) can be re-arranged a

$$\frac{V_m}{V_{bus}} = M \sqrt{\frac{2 \pi L_1 f_s}{4 n_t^2 D^2 R_L y}}$$
 W(17,b)

Therefore, using (12) and (17b), the proposed ac-dc converter gain is given by

$$\frac{Vr_o}{V_m} = \frac{Vr_o/V_{bus}}{V_m/V_{bus}} = \frac{M/2}{V_m/V_{bus}}.$$
 W(18)

Using the equations derived above, various design curves are obtained. Using (12) and (15), normalized halfbridge converter gain M versus phase-shift angle  $\theta$  for various values of normalized switching frequency F with Q = 0.9 is shown in Fig. 8(a). Similarly, Fig. 8(b) shows the converter gain M versus phase-shift angle  $\theta$  for various values of Q with normalized switching frequency F = 1.1. Using (12)-(16), the normalized peak tank current  $I_{rn,ru}$  and normalized peak capacitor voltage  $V_{Crp,pu}$  versus half-bridge converter gain M obtained are shown in Figs. 8(c) to (e), respectively. The tank kVA/kW of output power versus M for different values of Q is plotted in Fig. 8(f).

According to Figs. 8(a) and 8(b), M starts to increase, reaches its peak value and then decreases as the value of  $\theta$  is increased. Note that for the same value of  $\theta$ , smaller values of F and Q bring higher value of M. The proposed converter is supposed to operate in the rising part of the design curves to get enough gain since the converter should operate with wide variation (1:2) in input voltage. Figs. 8(c) to 8(e) show that smaller values of F and Q results in lower peak values for the resonant current and the resonant capacitor voltage. In Fig. 8(f), a smaller

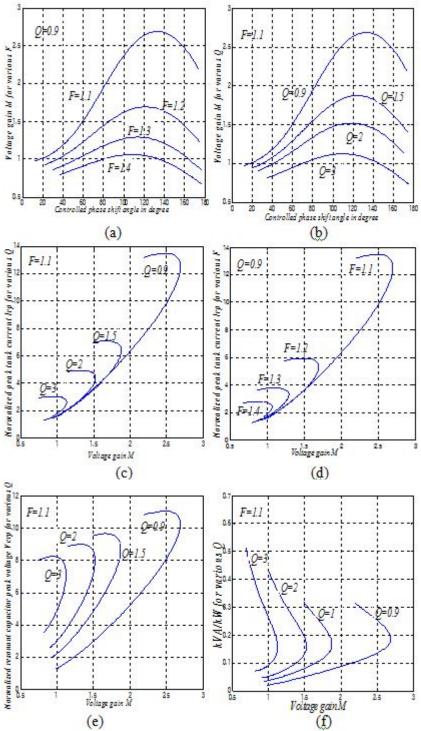


Figure 8. (a) Normalized voltage gain (M) vs phase shift  $\operatorname{angle}(\theta)$  for various values of normalized switching frequency F, (F=1.1 to 1.4), Q=0.9; (b) M vs phase shift angle for various values of Q (Q=0.9 to 3), F=1.1; (c) normalized tank peak current vs M for different values of Q (Q=0.9 to 3), F=1.1; (d) normalized tank peak current vs M for different values of P (P=1.1 to 1.4), P=0.9; (e) normalized peak capacitor voltage vs P=0.9 for various values of P=0.9 to 3), P=0.9; (f) tank P=0.9 to 3), value of P=0.9 to 3). value of P=0.9 to 3 to 3.

observations, optimum values chosen in the present design are F = 1.1 and Q = 0.9; dc-dc converter gain, M = 0.97.

IV. DESIGN EXAMPLE, SIMULATION AND EXPERIMETAL RESULTS

# A. Design

A design example with the following specifications is given to illustrate the design procedure: ac input voltage (peak value),  $V_m = 75-150 \text{ V}$ , 60Hz; output voltage,  $V_o = 100 \text{ V}$ ; output power,  $P_o = 100 \text{ W}$ ; switching frequency,  $f_s = 100 \text{ kHz}$ .

Using the equations given in [2,8]:  $V_B = V_{m,\text{max}} = 0.5 V_{bus,\text{max}} = 150 \text{ V}, D = 0.5, f_s = 100 \text{ kHz}, we calculate } L_1 = 248.88 \text{ mH}.$ 

In designing the converter, the optimum values chosen in Section III will be used, i.e., F = 1.1; Q = 0.9; and dc-dc converter gain, M = 0.97. It is also preferred that when the maximum input voltage is applied, the proposed converter is operating in Mode 2 to ensure the operation of switches in ZVS mode when phase-shift is applied.

Given  $I_o = P_o/V_o = 1$  A,  $R_L = V_o/I_o = 100$  W. Using (15) with  $\theta = \beta$  for Mode-2,  $\beta = 9.75^\circ$ . Hence the phase-shift must be adjusted to  $\theta = \beta = 9.75^\circ$  when the maximum input voltage is applied under full-load condition to ensure the converter operation in Mode 2. With the phase-shift increased, the converter operates in Mode 3.

On the primary-side of  $T_1$  reflected output voltage,  $V_o$ ' =  $MV_B = 145.5$  V, and the transformer ratio is  $n_t : 1 = V'_o : V_o = 1.455:1$ . The reflected load resistance value is  $R'_L = n_t^2 R_L = 211.7 \, \Omega$ . Based on (12), (17b) and other specifications in the example,  $V_m/V_{bus}$  as a function of  $\theta$  is plotted as Fig. 9, where M reaches its peak value M = 2.7 (Fig. 8(a) and (b)) at  $\theta = 130^\circ$  and using (17b) the corresponding value of  $V_m/V_{bus} = 0.66$ . Hence the maximum value of the proposed converter gain can be calculated using (18), which gives  $V'_o/V_m = 2.05$ . It is suitable for the wide input variation of the design example.

Using  $Q = 0.9 = \sqrt{L_r/C_r}/R'_L$  and  $F = 1.1 = \omega_s \sqrt{L_r C_r}$ , the tank parameters can be calculated as

$$L_r = 331.28 \,\mu\text{H}$$
 and  $C_r = 9.252 \,\text{nF}$ .

## B. PSIM Simulated Results

In order to verify design, the software PSIM 6.0 is used to simulate the design example. A fixed step of 0.1 µs is chosen for the simulation. The simulation results are shown for  $V_{\perp}$  = 150V (Fig. 9(a), Mode 2) and 75V (Fig. 9(b), Mode 3), respectively. When  $V_{m,\text{max}} = 150\text{V}$  is applied,  $\theta$  is set as  $6^{\circ}$  in order to make sure the proposed converter is operating in Mode 2. In Fig. 9(a), the secondary-side active rectifier works as a diode rectifier due to the current flowing through  $D_{\rm rd}/D_{\rm rd}$ as predicted. As expected,  $v_{rect}$  is a square wave. We observe a high power factor (0.99) and low total harmonic distortion (THD) (12.5%) for the input line current due to the DCM operation of  $i_{L1}$ .  $V_{bus}$  is twice of  $V_{m,max}$  because of the 50% duty cycle of front-end dual-switch boost converter operation. Also  $S_1/S_2$  operates in ZVS mode. When the minimum input voltage  $V_{m,min} = 75 \text{ V}$  is applied in Fig. 9(b),  $\theta$  is adjusted to 130° in order to obtain enough boost gain for regulating the output voltage.  $v_{rect}$  becomes a quasi-square wave due to operating interval 2,5,6 in Mode 3.  $V_{bus}$  is less than twice of  $V_{m,\min}$  as expected ( $V_m/V_{bus} = 0.66$  in Fig. 10). All switches work in ZVS mode. A lower power factor (0.87) and higher THD (56.2%) for the input line current are obtained since  $i_{II}$  loses DCM operation in parts of line frequency cycle. These waveforms confirm the theory.

Figure 9: Simulation results for (a)  $V_m = 150 \text{ V}$  and (b)  $V_m = 75 \text{ V}$ . Waveforms shown from top to bottom for each case: (i) line voltage, line current, bus voltage, load voltage; (ii) primary-side switch currents  $i_{O1}$  and  $i_{O2}$ , current through  $L_1$ 

 $(i_{L1})$ ; (iii) secondary-side switch currents  $i_{Q3}$  and  $i_{Q4}$ , rectified output current before filtering  $(i_o)$ ; (iv)  $v_{ab}$  and resonant current  $i_p$ , HF rectifier input voltage  $(v_{rect})$  and current  $(i_{rect})$ , resonant capacitor voltage  $(v_{ce})$ .

## C. Experiment Results

A 100 W laboratory prototype was built based on the design example presented above. The detailed values of MOSFET switches and passive components are listed in Table I. A DSP board (eZdspS320F2812) is used to generate phase-shifted PWM gating signals. The converter is operated in open-loop control for wide input voltage of 150V to 75V (peak). The experimental results are shown for  $V_m = 150$ V (Fig. 11(a), Mode 2) and 75V (Fig. 11(b), Mode 3), respectively. Input line voltage and line current waveforms together with HF waveforms are given in Fig. 11. Note that input pf = 0.98, THD = 17% at  $V_{m,max} = 150$ V,  $\theta = 10^{\circ}$ , and pf = 0.88, THD = 53.7% at  $V_{m,min} = 75$ V,  $\theta = 133^{\circ}$ . Comparing the simulated waveforms with the experimental ones, they are not much different, and these waveforms confirm the theory and simulated results.

Table II summarizes and compares theoretical, simulated and experimental results. Every group of data among theory, simulation and experiment is close enough.

#### V. Conclusions

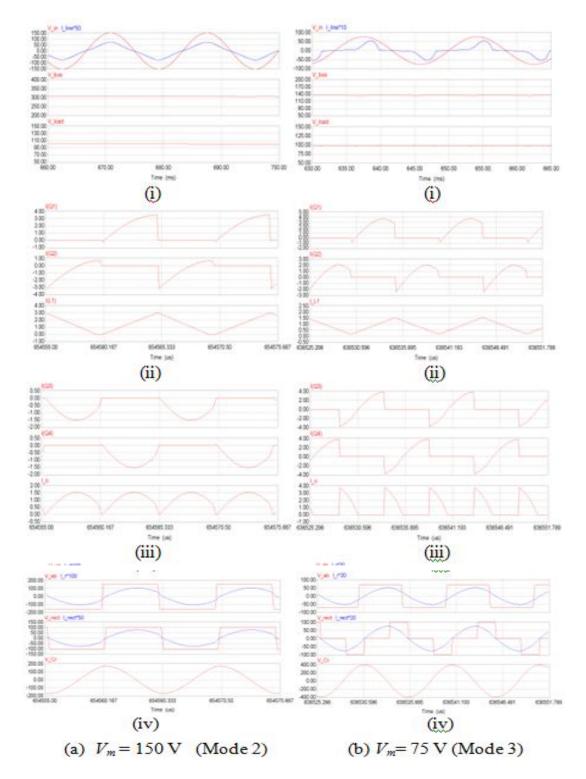
A new single-phase, single-stage active ac-dc converter is proposed and studied in this paper. The circuit is a single-stage configuration that integrates diode rectifier, boost chopper and HF isolated resonant dc-dc converter. Hence it includes functions of rectification, natural PFC (without active feedback control) and HF isolation, which is well suitable for several applications including PMSG-based small WECS. The output voltage is regulated by a fixed frequency, secondary-side phase-shift control strategy. All switches operate in soft-switching mode for the entire range of variations in input voltage due to the use of resonant converter and leakage inductance is used as part of resonant inductor.

The proposed converter operates in three modes depending on the conduction of different switches and diodes. The preferred Mode 2 and Mode 3 are analyzed using approximate ac circuit analysis approach. Design curves have been obtained using the analysis and a design example is presented to illustrate the design procedure. Using the values obtained in the design example, PSIM simulation and experiment were done and results obtained have been presented. The experimental results show good agreement with the theoretical analysis and simulated results. One problem with the proposed converter is low PF and higher THD for low line current. This problem will be solved in the future work.

Figure 11: Experiment results for (a)  $V_m = 150 \text{ V}$  and (b)  $V_m = 75 \text{ V}$ . Waveforms shown from top to bottom for each case: (i) line voltage (50V/div for (a), 20V/div for (b), ch4), line current (1A/div, ch3), time scale 2ms/div; (ii) FFT of input line current, 0.25A/div, 68.27Hz/div; (iii)  $v_{ab}$  (100V/div, ch1), HF rectifier input voltage  $v_{cont}$  (100V/div, ch2), resonant current  $i_r$  (1A/div

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for (a), 2.5A/div for (b), ch3); (iv) resonant capacitor voltage  $v_{cr}(100\text{V/div}, \text{ch4})$ ; (v) boost inductance current  $i_{L1}(1\text{A/div}, \text{ch3})$ , time scale in (iii)-(v): 2ms/div.



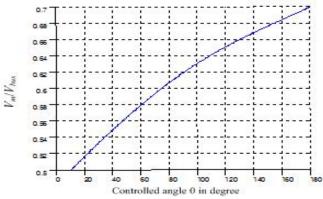


Figure 10.  $V_{\rm m}/V_{\rm bus}$  vs  $\theta$  (in degree) for the example (using numerical solution of (17b)).

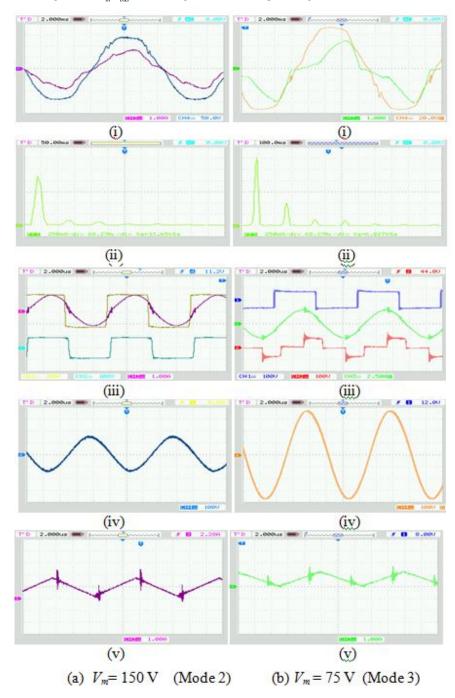


TABLE I.

COMPONENTS USED IN EXPERIMENT

$S_1/S_2, S_3/S_4$	MOSFETs: G20N50C, G22 N60S				
$D_1/D_2$ , $D_3/D_4$	U1560, RHRP1560				
$C_{bus}$ , $C_1$ , $C_2$ , $C_o$	400 μF				
$L_{\mathrm{l}}, L_{\mathrm{r}}^{**}, C_{r}$	248 μH, 310 μH*, 10.4nF				
$L_f, C_f$	3 mH, 1 μF				
HF transformer	Core: TDK EI60, material 2500B2				
	Tum s ratio: 14:10				

<sup>\*\*</sup>Including leakage inductance of HF transformer

TABLE II.

COMPARISON OF THEORETICAL, SIMULATED AND EXPERIMENTAL RESULTS

	$V_{m,max} = 150 \text{V (M ode 2)}$			$V_{m,min} = 75 \text{V (M ode 3)}$		
	theory	simn	expt	theory	si mn	expt
$I_{in, ms}$ (A)	-	0.965	0.98	-	2.49	2.1
pf	-	0.99	0.98	-	0.87	0.88
*THD(i li ne)	-	12.5%	17%	-	56.2%	53.7%
$V_o$ (V)	100	100.3	95.2	100	97.3	91.8
$V_{bus}\left(\mathbf{V}\right)$	300	305.9	296	113.6	131	114
θ	9.75°	6°	10 °	130°	130°	133°
$I_{r,pk}\left(\mathbf{A}\right)$	1.09	1.04	1.2	2.97	2.81	3.38
$V_{cr,pk}(V)$	134.7	168.6	150	363.7	398.2	368
efficiency	-	-	90%	-	-	86%

<sup>\*</sup>Using harmonic number up to 9

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